

一般相対性理論の数理：文献ガイド

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この追加資料では、本文中で著者名と発表年のみで引用した文献についてのより詳細な情報と、高次元ブラックホールに関する文献情報を参考資料として記載した。後者に関しては、著者が関心を持った文献の一部選んだもので、重要なものを網羅したものではないことをお断りしておく。

高次元関係と因果律関係を除いて、本文の構成に合わせて、テーマごとに文献を分け、それぞれのテーマ内では年代順に並べてある。本文での引用されている文献に対応する情報は、テーマ、年号、著者名をタグとして探して頂きたい。

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